

Weaker Forms of Monotonicity for Declarative Networking: a more fine-grained answer to the CALM-conjecture

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Introduction

- **Declarative Networking**: Datalog based languages for parallel and distributed computing
- **Cloud-computing**: Setting with asynchronous communication via messages which can be arbitrarily delayed but not lost
- **CALM-conjecture**: A query has a coordination-free and eventually consistent execution strategy iff the query is monotone

[Hellerstein, 2010]

CALM = Consistency And Logical Monotonicity

CALM

[Ameloot, Neven, Van den Bussche, 2011]

A query has a coordination-free and eventually consistent execution strategy
iff
the query is monotone

⇓
Theorem
 $\mathcal{F}_0 = \mathcal{M}$

CALM-conjecture

- [Ameloot, Neven, Van den Bussche, 2011]: TRUE
for a setting where nodes have **no** information about the distribution of facts
- [Zinn, Green, Ludäscher, 2012]: FALSE
for settings where nodes **have** information about the distribution of facts
- **TRUE when also refining monotonicity**

CALM Revision 1

A query has a coordination-free and eventually consistent execution strategy *under distribution policies*
iff
the query is *domain-distinct-monotone*

⇓
Theorem
 $\mathcal{F}_1 = \mathcal{M}_{distinct}$

Summary

\mathcal{F}_0	$\stackrel{!}{=}$	\mathcal{M}	$\stackrel{!}{=}$	wLOG(\neq)	$\stackrel{!}{\supseteq}$	Datalog(\neq)
\mathcal{F}_1	$\stackrel{!}{=}$	$\mathcal{M}_{distinct}$	$\stackrel{!}{=}$	SP-wLOG	$\stackrel{!}{\supseteq}$	SP-Datalog
\mathcal{F}_2	$\stackrel{!}{=}$	$\mathcal{M}_{disjoint}$	$\stackrel{!}{=}$	semicon-wLOG [⊃]	$\stackrel{!}{\supseteq}$	semicon-Datalog [⊃]
Coordination freeness		Monotonicity		Datalog + value invention		Datalog

CALM Revision 2

A query has a coordination-free and eventually consistent execution strategy *under domain-guided distribution policies*
iff
the query is *domain-disjoint-monotone*

⇓
Theorem
 $\mathcal{F}_2 = \mathcal{M}_{disjoint}$

Monotonicity

Definition

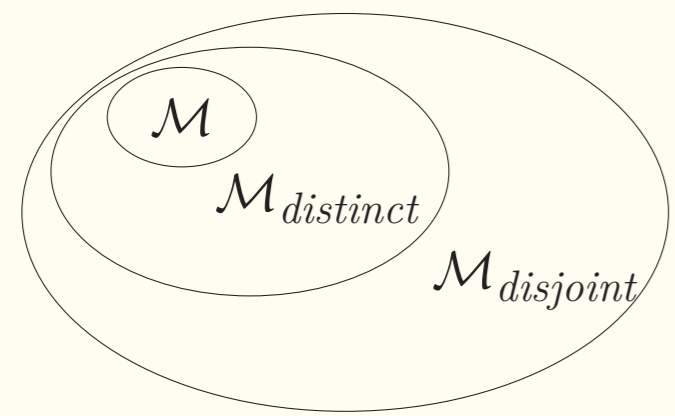
A query Q is **monotone** if $Q(\mathbf{I}) \subseteq Q(\mathbf{I} \cup \mathbf{J})$ for all database instances \mathbf{I} and \mathbf{J} .

Notation

\mathcal{M} : class of monotone queries

Example

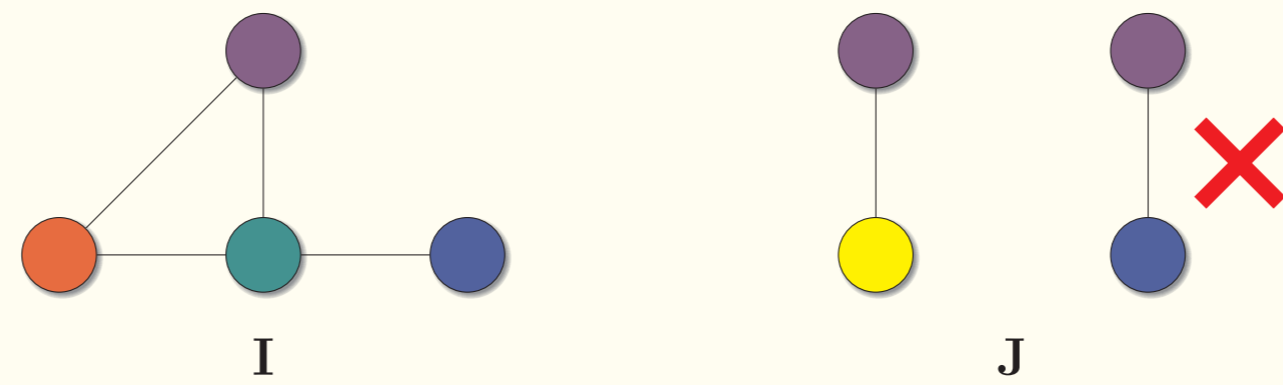
- Select triangles in a graph $\in \mathcal{M}$
- Select open triangles in a graph $\notin \mathcal{M}$



Domain-distinct-monotonicity

- A fact \mathbf{f} is **domain distinct** from instance \mathbf{I} when $adom(\mathbf{f}) \not\subseteq adom(\mathbf{I})$.
- An instance \mathbf{J} is **domain distinct** from instance \mathbf{I} when every fact $\mathbf{f} \in \mathbf{J}$ is domain distinct from \mathbf{I} .

Example



Definition

A query Q is **domain-distinct-monotone** if $Q(\mathbf{I}) \subseteq Q(\mathbf{I} \cup \mathbf{J})$ for all \mathbf{I} and \mathbf{J} for which \mathbf{J} is domain distinct from \mathbf{I} .

Notation

$\mathcal{M}_{distinct}$: class of **domain-distinct-monotone** queries

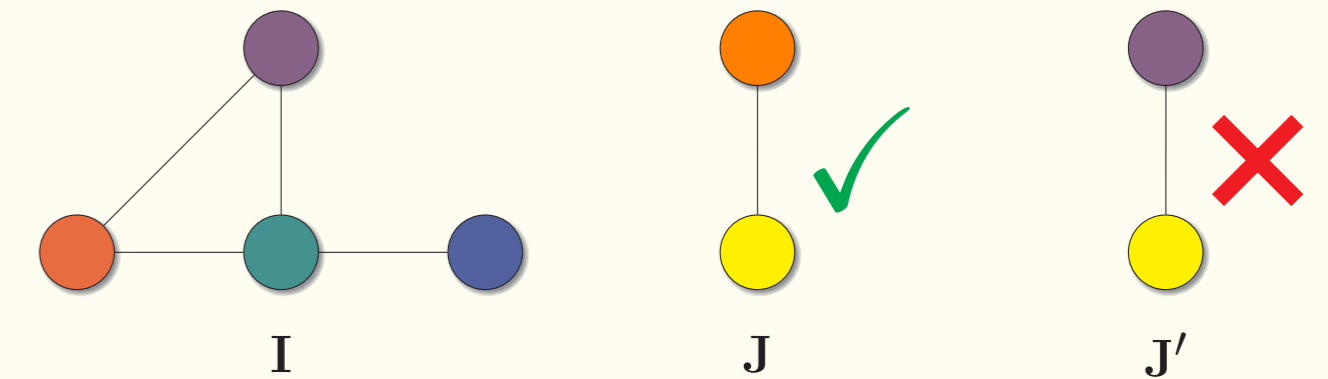
Remark

$\mathcal{M}_{distinct}$: class of queries preserved under extensions

Domain-disjoint-monotonicity

- An instance \mathbf{J} is **domain disjoint** from instance \mathbf{I} when $adom(\mathbf{I}) \cap adom(\mathbf{J}) = \emptyset$.

Example



Definition

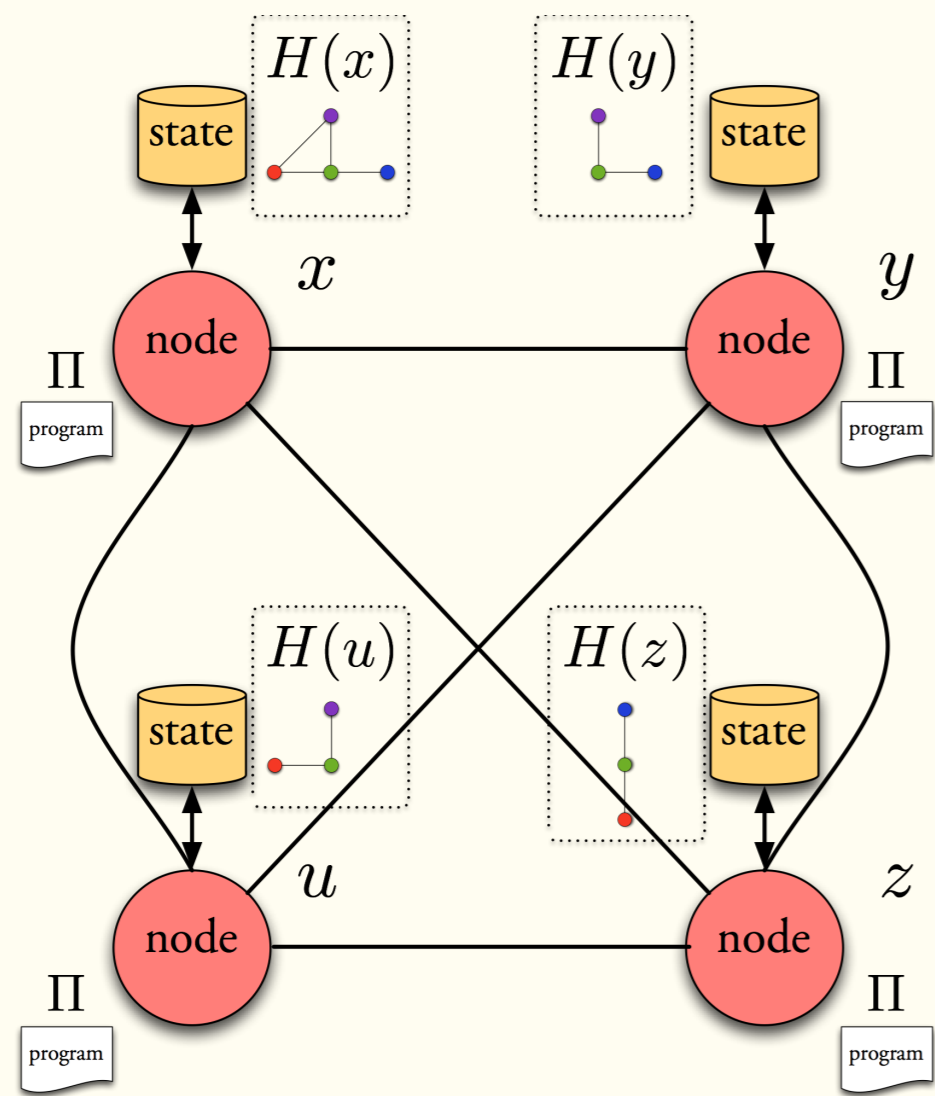
A query Q is **domain-disjoint-monotone** if $Q(\mathbf{I}) \subseteq Q(\mathbf{I} \cup \mathbf{J})$ for all \mathbf{I} and \mathbf{J} for which \mathbf{J} is domain disjoint from \mathbf{I} .

Notation

$\mathcal{M}_{disjoint}$: class of **domain-disjoint-monotone** queries

Relational Transducer Networks

- Network $\mathcal{N} = \{x, y, u, z\}$
- Transducer Π
- messages can be arbitrarily delayed but never get lost



Semantics defined in terms of runs over a transition system

Definition

A transducer Π **computes** a query Q if

- for all networks \mathcal{N} , **Network independent**
- for all databases \mathbf{I} , **Data distribution independent**
- for all horizontal distributions H , and
- for every run of Π ,

$$out(\Pi) = Q(\mathbf{I}).$$

Consistency requirement

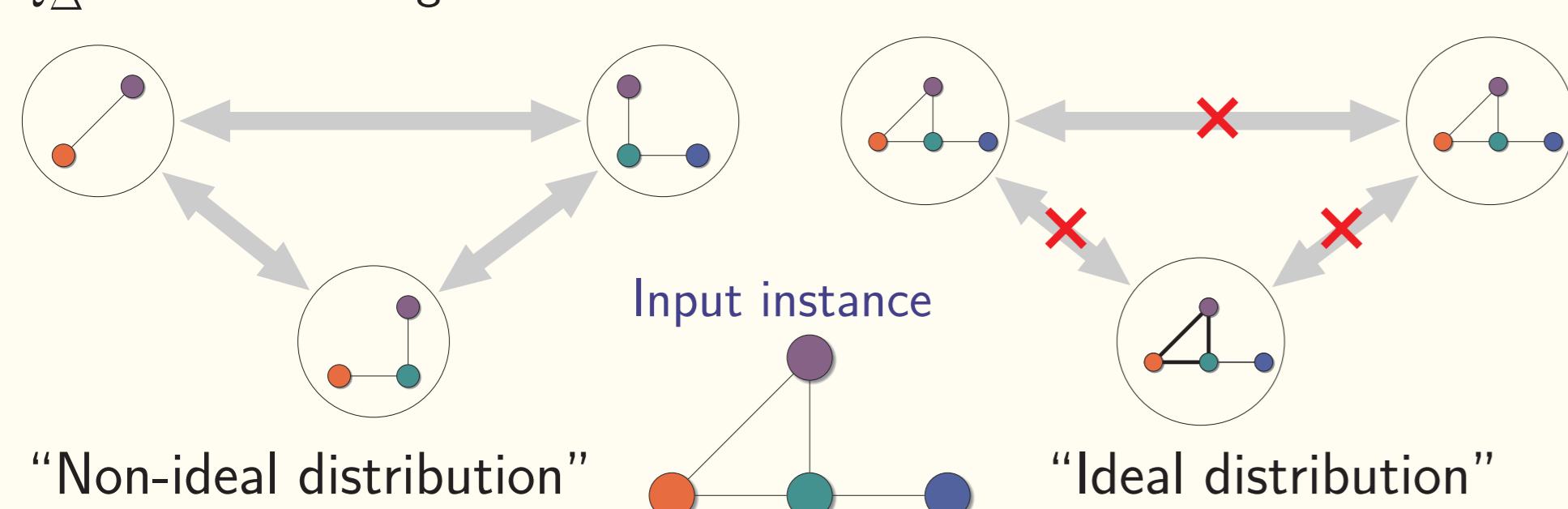
Definition

Π is **coordination-free** if for all inputs \mathbf{I} there is a distribution on which Π computes $Q(\mathbf{I})$ without having to do communication.

Goal: separate data-communication from coordination-communication

Example

Q_{Δ} : select all triangles $\in \mathcal{M}$

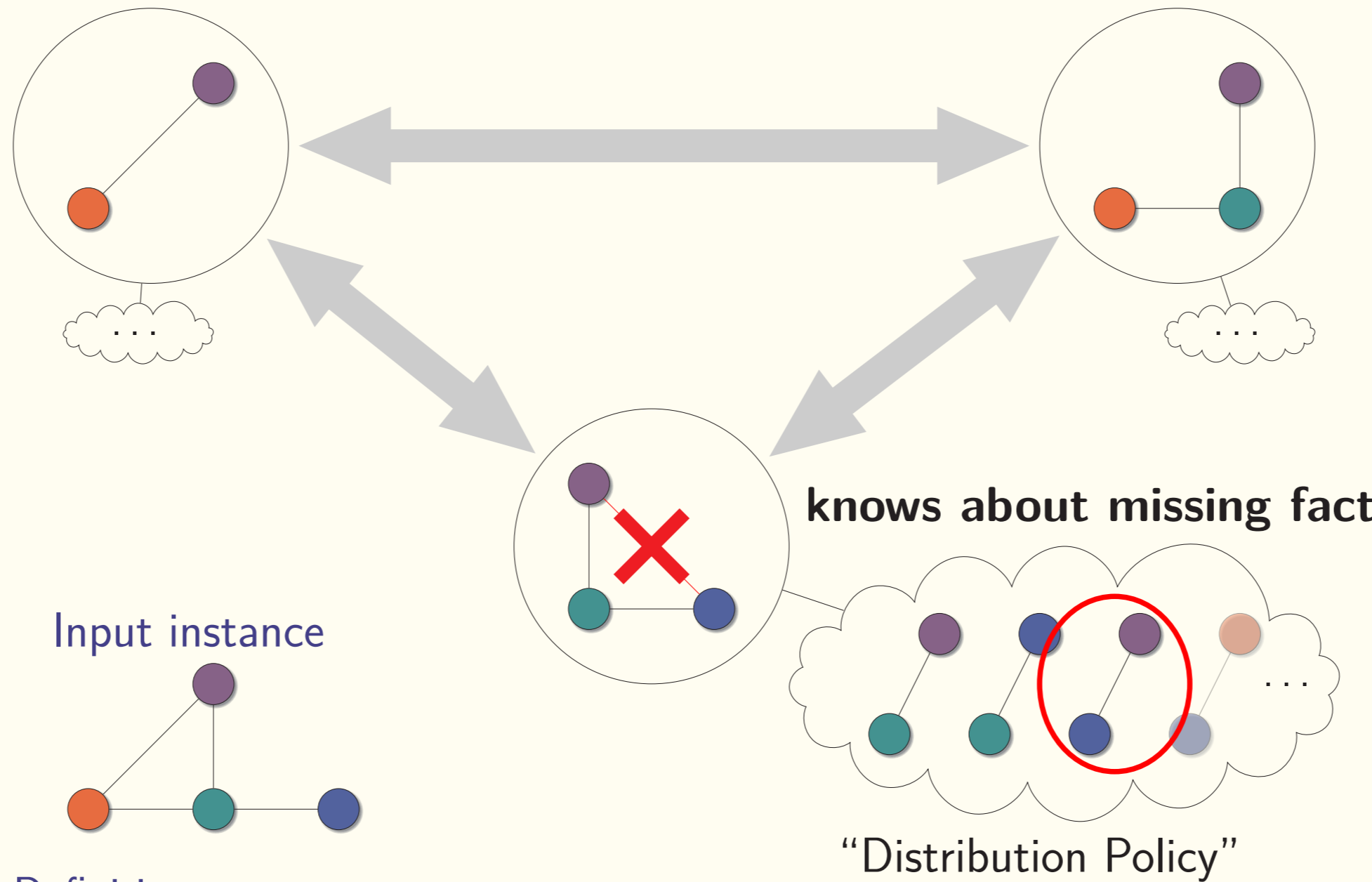


Definition

\mathcal{F}_0 = set of queries which are distributedly computed by coordination-free transducers.

Policy-aware Transducers

[Zinn, Green, Ludäscher, 2012]



Definition

- A **distribution policy** \mathbf{P} for σ and \mathcal{N} is a total function from $facts(\sigma)$ to the power set of \mathcal{N} (where $\mathbf{P}(\mathbf{f}) \neq \emptyset$, for every fact \mathbf{f}).
- A **policy-aware** transducer is a transducer with access to \mathbf{P} restricted to its active domain.

Intuition

- every node is responsible for a predetermined set of facts
- every fact \mathbf{f} in the global instance appears on all nodes responsible for \mathbf{f}

Definition

A **policy-aware** transducer Π **computes** a query Q if

- for all networks \mathcal{N} ,
- for all databases \mathbf{I} ,
- for all **distribution policies** \mathbf{P} , and
- for every run of Π ,

$$out(\Pi) = Q(\mathbf{I}).$$

Definition

\mathcal{F}_1 = set of queries which are distributedly computed by policy-aware coordination-free transducers.

Proof of $\mathcal{M}_{distinct} \subseteq \mathcal{F}_1$

Observation

Let \mathbf{I} be an instance, $C \subseteq adom(\mathbf{I})$.

Induced instance: $\mathbf{I}|_C = \{\mathbf{f} \in \mathbf{I} \mid adom(\mathbf{f}) \subseteq C\}$

By domain-distinct-monotonicity: $Q(\mathbf{I}|_C) \subseteq Q(\mathbf{I})$

C is **complete** at node x when x knows for every fact \mathbf{f} with $adom(\mathbf{f}) \subseteq C$ whether $\mathbf{f} \in \mathbf{I}$ or $\mathbf{f} \notin \mathbf{I}$.

Algorithm

- broadcast all positive **and negative** facts
- Evaluate query on **complete** sets

Semi-positive Datalog

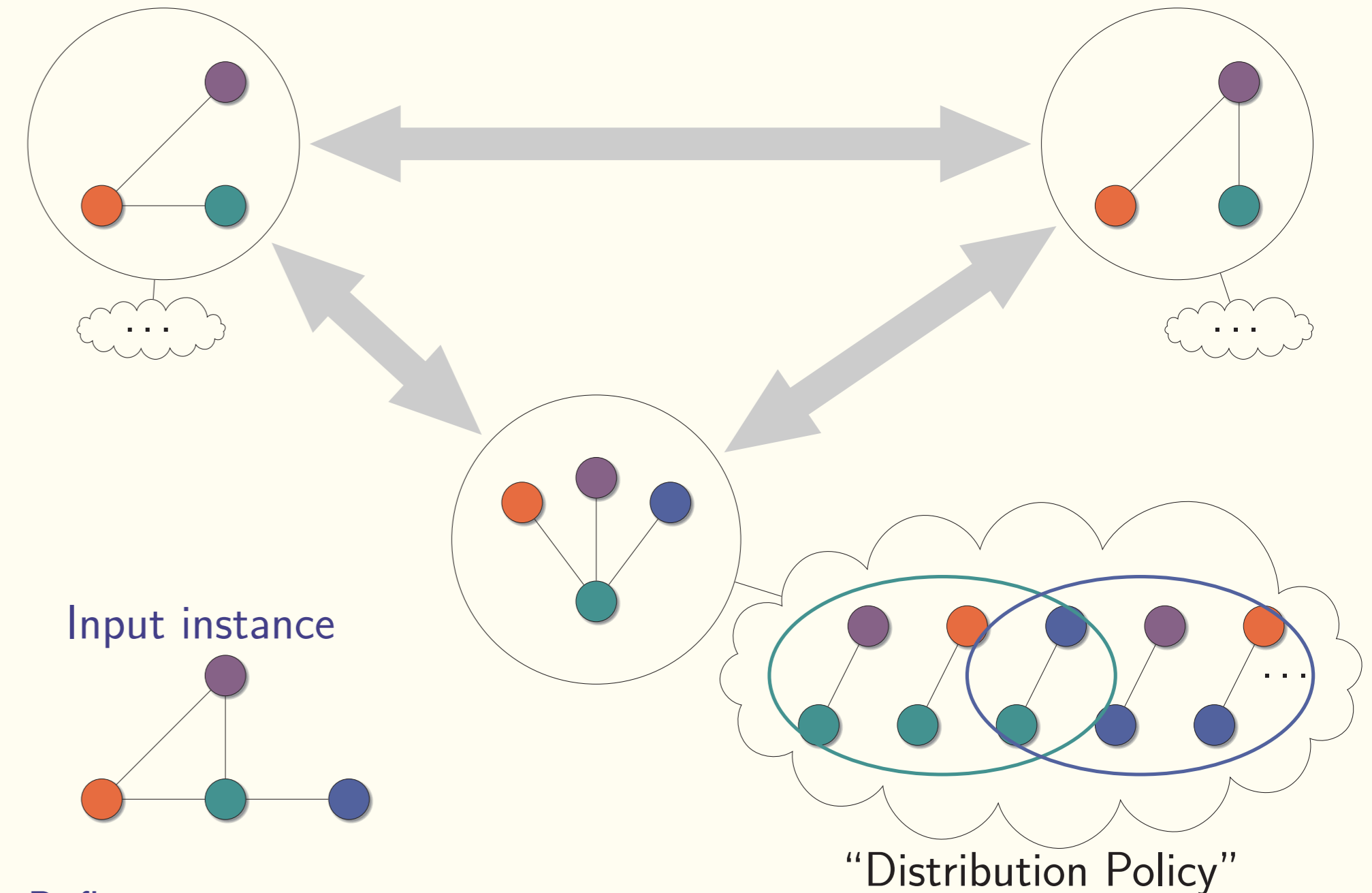
SP-Datalog \subsetneq SP-wLOG = $\mathcal{M}_{distinct}$

► SP-Datalog $\subsetneq \mathcal{M}_{distinct} \cap \text{PTIME}$

► SP-wLOG = $\mathcal{M}_{distinct}$

Domain-guided Policies

[Zinn, Green, Ludäscher, 2012]



Definition

- A **domain assignment** α for \mathcal{N} is a total function from dom to the power set of \mathcal{N} .
- A distribution policy \mathbf{P} is **domain-guided** if there is a domain assignment α where

$$\mathbf{P}(R(a_1, \dots, a_k)) = \bigcup_{i=1}^k \alpha(a_i).$$

Intuition

- every node is responsible for a predetermined set of domain elements
- every fact $R(a_1, \dots, a_k)$ in the global instance appears on all nodes responsible for at least one value a_i (with $i \in \{1, \dots, k\}$)

Definition

\mathcal{F}_2 = queries which are distributedly computed under **domain-guided** distribution policies by policy-aware **coordination-free** transducers.

Semiconnected Datalog

semicon-Datalog[⊃] \subsetneq semicon-wLOG[⊃] = $\mathcal{M}_{disjoint}$

Connected Rules

$O(x, y, z) \leftarrow E(x, y), E(y, z), E(z, x)$ is connected
 $O(x, y, z) \leftarrow E(x, y), E(z, z)$ is not connected

Definition

A stratified-Datalog program is **semi-connected** if all rules are connected except (possibly) those of the last stratum.

Example

$$\begin{aligned} TC(x, y) &\leftarrow E(x, y) \\ TC(x, y) &\leftarrow E(x, z), TC(z, y) \\ O(x, y) &\leftarrow \neg TC(x, y), x \neq y \end{aligned}$$

Conclusion and Future Work

Conclusion

- Coordination-free evaluation = (refined) monotonicity
- Introduction of (semi-)connected Datalog

Can we put the CALM-conjecture to rest?

Future Work

- Other settings / other distribution policies?
- Coordination-free + efficient evaluation?

Positive Datalog with inequalities

Datalog(\neq) \subsetneq wLOG(\neq) = \mathcal{M}

► Datalog(\neq) $\subsetneq \mathcal{M} \cap \text{PTIME}$

[Afrati, Cosmadakis, Yannakakis, 1994]

► wLOG(\neq) = \mathcal{M}

[Cabibbo, 1998]

[Afrati, Cosmadakis, Yannakakis, 1994]

[Cabibbo, 1998]